



Dr. Bbosa Science

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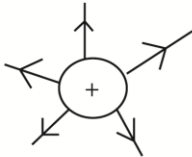
Electric field

An electric field is a region around an electric charge where an electric force is experienced. This can be mapped out by electrostatic lines of force.

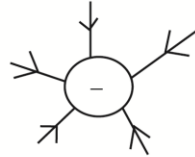
A line of force is a line such that the tangent to it at any point is in the direction of the force on a small positive charge at that point. Arrows are drawn the direction and these point from positive towards or inwards to the negative charge. A collection of lines of force is called an **electric flux**.

Electric field pattern

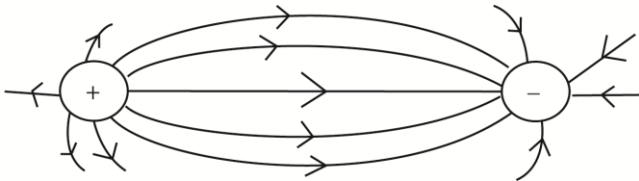
1. Isolated positive charge



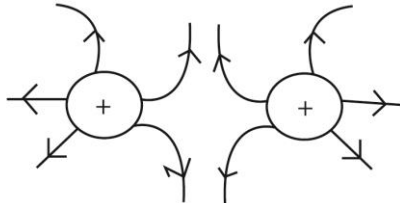
2. Isolated negative charge



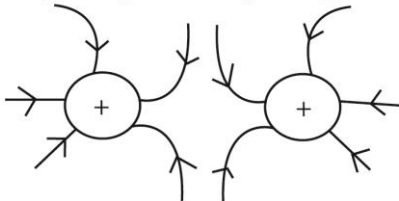
3. Two equal unlike charges



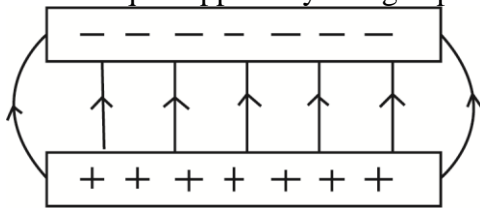
4. Two equal positive charges magnitudes



5. Two equal negative charges magnitudes



6. Two equal oppositely charged parallel plates



Definition

1. A neutral point in an electric field is a point where the resultant electric field intensity is zero.

The force exerted on the charged body in an electric field depends on the charge on the body and the intensity or strength of the field.

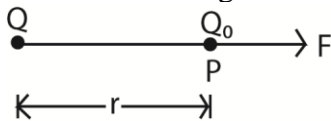
2. Electric field intensity or strength is defined as the force exerted on a positive charge of 1 coulomb placed at a point in electric field

Therefore, electric field intensity, E is a vector quantity

$$E = \frac{F}{Q}$$

The S.I. unit of E is NC^{-1}

Consider the diagram below



Placing a small charge Q_0 at point P, in an electric field, the force at P due to Q is given by

$$F = \frac{1}{4\pi\epsilon_0} \times \frac{QQ_0}{r^2}$$

$$\begin{aligned} \text{Electric field intensity, } E, \text{ at P} &= \frac{F}{Q_0} \\ &= \frac{Q}{4\pi\epsilon_0 r^2} \end{aligned}$$

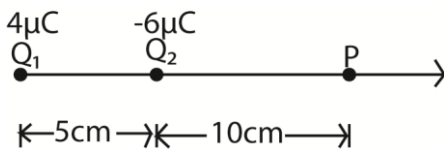
Therefore electric field intensity, E , at a point due to charge Q is given by

$$E = \frac{Q}{4\pi\epsilon_0 r^2}$$

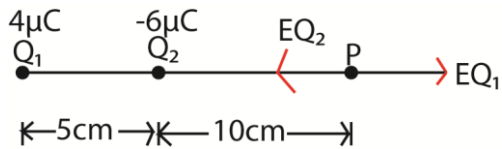
Note E is directed away from a positive charge and directed towards the negative charge.

Example 1

Find the electric field intensity at P



Solution



Solution

E at P due to Q_1

$$E_{Q_1} = \frac{9.0 \times 10^9 \times 4 \times 10^{-6}}{(15 \times 10^{-2})^2} = 16 \times 10^5 \text{NC}^{-1} (\rightarrow)$$

E at P due to Q_2

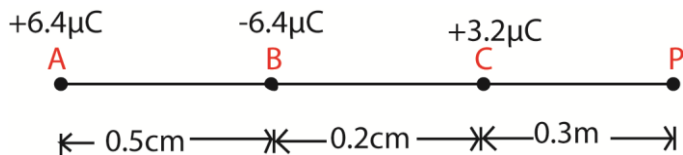
$$E_{Q_2} = \frac{9.0 \times 10^9 \times 4 \times 10^{-6}}{(10 \times 10^{-2})^2} = 54 \times 10^5 \text{NC}^{-1} (\leftarrow)$$

$$E_P = E_{Q_1} - E_{Q_2}$$

$$= (16 \times 10^5 - 54 \times 10^5) \text{NC}^{-1}$$

$$= -38 \times 10^5 \text{NC}^{-1} (\leftarrow)$$

Example 2



Three point charges of $+6.4\mu\text{C}$, $-6.4\mu\text{C}$ and $+3.2\mu\text{C}$ are arranged in line at points A , B , and C respectively as shown in diagram above. Find the electric field intensity at P .

Solution

E at P due to A ($+6.4\mu\text{C}$)

$$E_{AP} = \frac{9.0 \times 10^9 \times 6.4 \times 10^{-6}}{(1)^2} = 5.76 \times 10^4 \text{NC}^{-1} (\rightarrow) (\text{repulsive})$$

E at P due to B ($-6.4\mu\text{C}$)

$$E_{BP} = \frac{9.0 \times 10^9 \times 6.4 \times 10^{-6}}{(0.5)^2} = 2.304 \times 10^5 \text{NC}^{-1} (\leftarrow) (\text{attractive})$$

E at P due to C ($+3.2\mu\text{C}$)

$$E_{CP} = \frac{9.0 \times 10^9 \times 3.2 \times 10^{-6}}{(0.3)^2} = 3.2 \times 10^5 \text{NC}^{-1} (\rightarrow) (\text{repulsive})$$

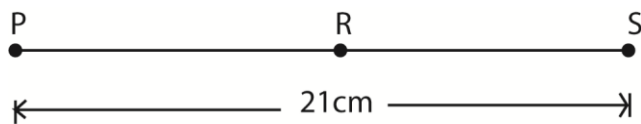
$$E_P = E_{AP} - E_{BP} + E_{CP}$$

$$= (5.76 \times 10^4 - 2.30 \times 10^5 + 3.2 \times 10^5) \text{NC}^{-1}$$

$$= 1.472 \times 10^5 \text{NC}^{-1} (\rightarrow)$$

Hence the electric field at P is $1.472 \times 10^5 \text{ NC}^{-1}$ to the right

Example 3



Two point Charges P and S of $-17.6 \mu\text{C}$ and $-9.0 \mu\text{C}$ respectively are placed in a vacuum at a distance of 21 cm apart. When a 3rd charge R is placed midway between P and S as shown in figure above, then, the net force at S is zero

- (i) Determine the charge on R
- (ii) Calculate the electric potential at position R.
- (iii) Sketch the electric field lines corresponding to charge distribution

Solution

Let the charge on R be Q

From

$$F = \frac{1}{4\pi\epsilon_0} \times \frac{QQ_0}{r^2} \text{ where } \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9$$

Force on S due to R

$$F_{SR} = \frac{9.0 \times 10^9 \times 9 \times 10^{-6} \times Q}{(10.5 \times 10^{-2})^2}$$

Force on S due to P

$$F_{SP} = \frac{9.0 \times 10^9 \times 9 \times 10^{-6} \times 17.6 \times 10^{-6}}{(21 \times 10^{-2})^2}$$

Resultant force on S = $F_{SP} - F_{SR} = 0$

$$\Rightarrow F_{SP} = F_{SR}$$

$$\frac{9.0 \times 10^9 \times 9 \times 10^{-6} \times 17.6 \times 10^{-6}}{(21 \times 10^{-2})^2} = \frac{9.0 \times 10^9 \times 9 \times 10^{-6} \times Q}{(10.5 \times 10^{-2})^2}$$

$$Q = \frac{17.6 \times 10^{-6} \times (10.5 \times 10^{-2})^2}{(21 \times 10^{-2})^2} = 4.4 \times 10^{-6} \text{ C}$$

Hence the charge on R = $+4.4 \times 10^{-6} \text{ C}$

(ii) Electric field potential, at a distance r from charge D is given by

$$V = \frac{Q}{4\pi\epsilon_0 r}$$

Electric potential at R due to S

$$V_{RS} = \frac{9 \times 10^9 \times -9 \times 10^{-6}}{10.5 \times 10^{-2}} = -7.71 \times 10^5 \text{ V}$$

Electric potential at R due to P

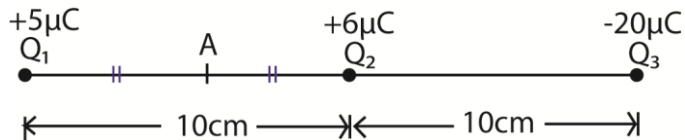
$$V_{RP} = \frac{9 \times 10^9 \times -17.6 \times 10^{-6}}{x \times 10.5 \times 10^{-2}} = -1.51 \times 10^6 \text{V}$$

$$V_R = V_{RS} + V_{RP}$$

$$= -7.71 \times 10^5 + -1.51 \times 10^6$$

$$= -2.28 \times 10^6 \text{V}$$

Example 4



Calculate the electric field intensity midway between \$Q_1\$ and \$Q_2\$

Solution

$$\text{From } E = \frac{Q}{4\pi\epsilon_0 r^2}$$

$$E_{Q_1} \text{ at A due to } Q_1 (= \frac{9 \times 10^9 \times 5 \times 10^{-6}}{(5 \times 10^{-2})^2}) = 1.8 \times 10^7 \text{NC}^{-1} (\leftarrow)$$

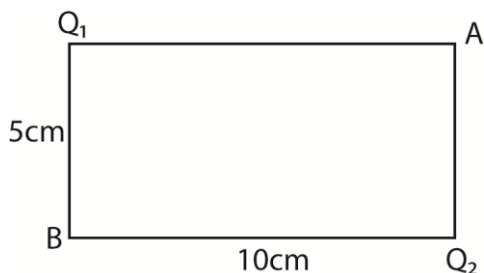
$$E_{Q_2} \text{ at A due to } Q_2 = \frac{9 \times 10^9 \times 6 \times 10^{-6}}{(5 \times 10^{-2})^2} = 2.16 \times 10^7 \text{NC}^{-1} (\leftarrow)$$

$$E_{Q_3} \text{ at A due to } Q_3 = \frac{9 \times 10^9 \times 20 \times 10^{-6}}{(15 \times 10^{-2})^2} = 8.0 \times 10^6 \text{NC}^{-1} (\rightarrow)$$

$$\begin{aligned} E_A &= E_{Q_1} - E_{Q_2} + E_{Q_3} \\ &= 1.8 \times 10^7 - 2.16 \times 10^7 + 8.0 \times 10^6 \\ &= 4.4 \times 10^6 \text{NC}^{-1} (\rightarrow) \end{aligned}$$

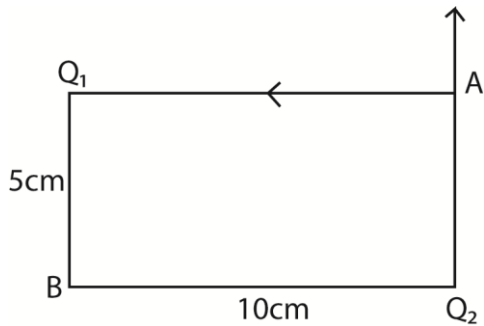
Example 5

Charges \$Q_1\$ and \$Q_2\$ of \$-5\mu\text{C}\$ and \$+2.0\mu\text{C}\$ respectively are placed at two opposite corners of a rectangle of sides \$5.0\text{cm}\$ and \$10.0\text{cm}\$ as shown below



Calculate the electric field at \$A\$

Solution



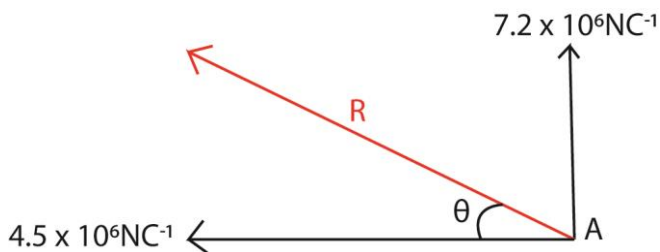
$$\text{From } E = \frac{Q}{4\pi\epsilon_0 r^2}, \text{ and } E = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9$$

E at A due to Q1

$$E_{Q_1} = \frac{9 \times 10^9 \times 5 \times 10^{-6}}{(10 \times 10^{-2})^2} = 4.5 \times 10^6 \text{NC}^{-1}$$

E at A due to Q2

$$E_{Q_2} = \frac{9 \times 10^9 \times 2 \times 10^{-6}}{(5 \times 10^{-2})^2} = 7.2 \times 10^6 \text{NC}^{-1}$$



$$R^2 = (4.5 \times 10^6)^2 + (7.2 \times 10^6)^2$$

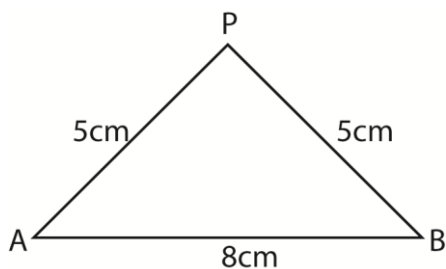
$$R = 8.49 \times 10^6 \text{NC}^{-1}$$

$$\tan \theta = \frac{7.2 \times 10^6}{4.5 \times 10^6}$$

$$\theta = 58^\circ$$

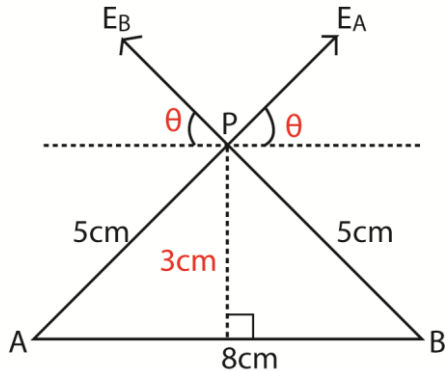
Hence the electric field intensity at A is $8.49 \times 10^6 \text{NC}^{-1}$ at 58° to the horizontal

Example 6



Two point charges A and B of $+10\mu\text{C}$ and $+0.05\mu\text{C}$ are separated by a distance of 8cm along the horizontal as shown above. Find the electric field intensity at P.

Solution



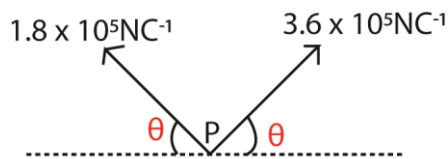
$$\sin \theta = \frac{3}{5} = 0.6; \quad \cos \theta = \frac{4}{5} = 0.8$$

E at P due to charge at A

$$E_{Q_1} = \frac{9 \times 10^9 \times 0.1 \times 10^{-6}}{(5 \times 10^{-2})^2} = 3.6 \times 10^5 \text{NC}^{-1}$$

E at A due to charge at B

$$E_{Q_2} = \frac{9 \times 10^9 \times 0.05 \times 10^{-6}}{(5 \times 10^{-2})^2} = 1.8 \times 10^5 \text{NC}^{-1}$$

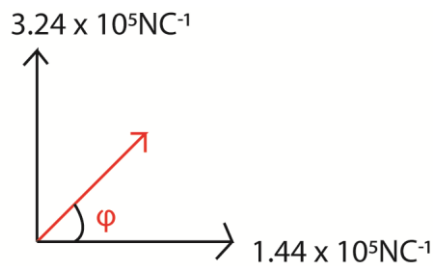


Resolving vertically

$$\begin{aligned} E_y &= 3.6 \times 10^5 \sin \theta + 1.8 \times 10^5 \sin \theta \\ &= 5.4 \times 10^5 \sin \theta \\ &= 5.4 \times 0.6 = 3.24 \times 10^5 \text{NC}^{-1} \end{aligned}$$

Resolving horizontally

$$\begin{aligned} E_x &= 3.6 \times 10^5 \cos \theta - 1.8 \times 10^5 \cos \theta \\ &= 1.8 \times 10^5 \times 0.8 \\ &= 1.44 \times 10^5 \text{NC}^{-1} \end{aligned}$$



$$R^2 = (1.44 \times 10^5)^2 + (3.24 \times 10^5)^2$$

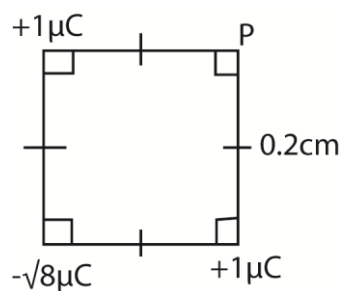
$$R = 3.55 \times 10^5 \text{ NC}^{-1}$$

$$\tan \theta = \frac{3.24 \times 10^6}{1.44 \times 10^6}$$

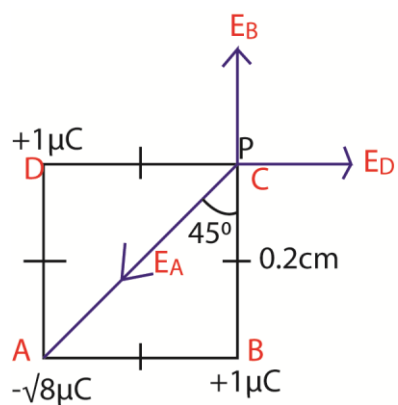
$$\theta = 66^\circ$$

Hence the electric field intensity at A is $3.55 \times 10^5 \text{ NC}^{-1}$ at 66° to the horizontal

Example 7



Solution



$$AP^2 = 0.2^2 + 0.2^2$$

$$AP = \sqrt{8} \times 10^{-1} \text{ m}$$

E at P due to charge at A

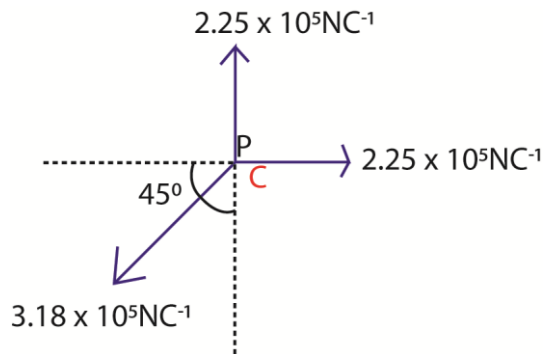
$$E_A = \frac{9 \times 10^9 \times \sqrt{8} \times 10^{-6}}{(\sqrt{8} \times 10^{-1})^2} = 3.18 \times 10^5 \text{ NC}^{-1}$$

E at P due to charge at B

$$E_{Q_2} = \frac{9 \times 10^9 \times 1 \times 10^{-6}}{(0.2)^2} = 2.25 \times 10^5 \text{NC}^{-1}$$

E at P due to charge at D

$$E_{Q_2} = \frac{9 \times 10^9 \times 1 \times 10^{-6}}{(0.2)^2} = 2.25 \times 10^5 \text{NC}^{-1}$$

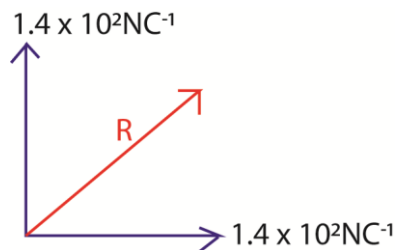


Resolving vertically

$$E_y = 2.25 \times 10^5 - 3.18 \times 10^5 \sin 45^\circ = 1.4 \times 10^2 \text{NC}^{-1}$$

Resolving horizontally

$$E_x = 2.25 \times 10^5 - 3.18 \times 10^5 \sin 45^\circ = 1.4 \times 10^2 \text{NC}^{-1}$$



$$R^2 = (1.4 \times 10^2)^2 + (1.4 \times 10^2)^2$$

$$R = 1.98 \times 10^2 \text{NC}^{-1}$$

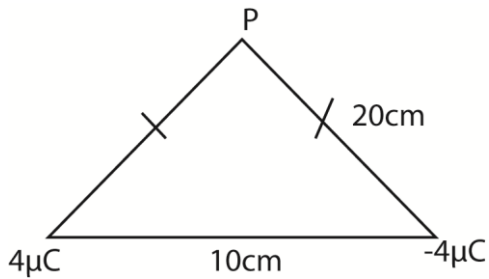
$$\tan \theta = \frac{1.4 \times 10^2}{1.4 \times 10^2}$$

$$\theta = 45^\circ$$

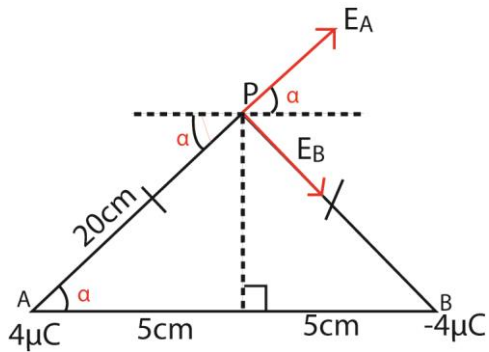
Hence the electric field intensity at P is $1.98 \times 10^2 \text{NC}^{-1}$ at 45° to horizontal

Example 8

Two point charges are separated by 10cm in air as shown



Solution

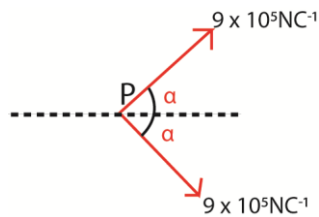


E at P due to charge at A

$$E_A = \frac{9 \times 10^9 \times 4 \times 10^{-6}}{(20 \times 10^{-2})^2} = 9 \times 10^5 \text{NC}^{-1}$$

E at P due to charge at B

$$E_B = \frac{9 \times 10^9 \times 4 \times 10^{-6}}{(20 \times 10^{-2})^2} = 9 \times 10^5 \text{NC}^{-1}$$



$$\sin \alpha = \frac{\sqrt{375}}{20}; \cos \alpha = \frac{5}{20} = 0.25$$

Resolving vertically

$$E_y = 9 \times 10^5 \text{NC}^{-1} \sin \alpha - 9 \times 10^5 \text{NC}^{-1} \sin \alpha = 0$$

Resolving horizontally

$$E_x = 9 \times 10^5 \text{NC}^{-1} \cos \alpha + 9 \times 10^5 \text{NC}^{-1} \cos \alpha$$

$$= 18 \times 10^5 \times .25 = 4.5 \times 10^5 \text{NC}^{-1}$$

$$R^2 = (4.5 \times 10^5)^2 + (0)^2$$

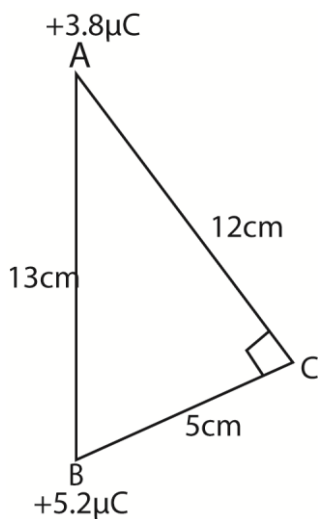
$$R = 4.5 \times 10^5 \text{ NC}^{-1}$$

$$\tan \theta = \frac{0}{4.5 \times 10^5}$$

$$\theta = 0^\circ$$

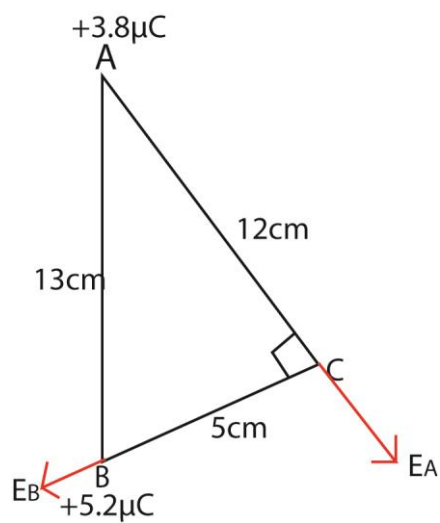
Hence the electric field intensity at P is $4.5 \times 10^5 \text{ NC}^{-1}$ at 0° to the horizontal

Example 9



Two points $+3.8\mu\text{C}$ and $-5.2\mu\text{C}$ are placed in air at points A and B as shown. Determine the electric field intensity at C

Solution

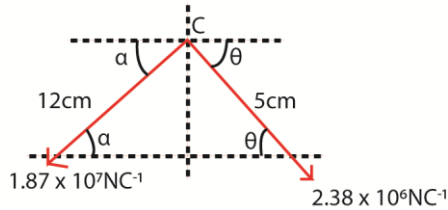


E at C due to charge at A

$$E_A = \frac{9 \times 10^9 \times 3.8 \times 10^{-6}}{(12 \times 10^{-2})^2} = 2.38 \times 10^5 \text{NC}^{-1}$$

E at C due to charge at B

$$E_B = \frac{9 \times 10^9 \times 5.2 \times 10^{-6}}{(5 \times 10^{-2})^2} = 1.87 \times 10^7 \text{NC}^{-1}$$



$$\tan \alpha = \frac{5}{12}; \alpha = 22.6 \quad \tan \theta = \frac{12}{5}; \theta = 67.4$$

Resolving vertically;

$$E_y = 1.87 \times 10^7 \sin 22.6 + 2.38 \times 10^6 \sin 67.4$$

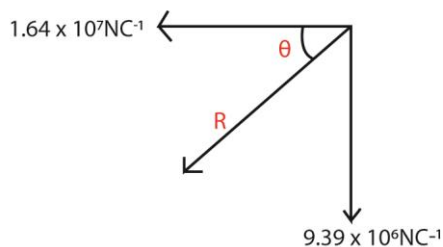
$$= 9.39 \times 10^6 \text{NC}^{-1}$$

Resolving horizontally

$$E_x = 2.38 \times 10^6 \cos 67.4 - 1.87 \times 10^7 \cos 22.6$$

$$= 9.16 \times 10^6 - 1.73 \times 10^7$$

$$= -1.64 \times 10^7 \text{NC}^{-1}$$



$$R^2 = (1.64 \times 10^7)^2 + (9.39 \times 10^6)^2$$

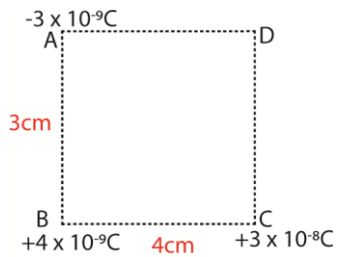
$$R = 1.89 \times 10^7 \text{NC}^{-1}$$

$$\tan \theta = \frac{9.39 \times 10^6}{1.64 \times 10^7}$$

$$\theta = 29.79^\circ$$

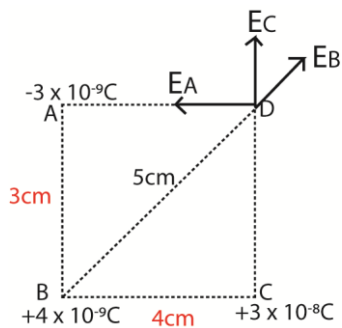
Hence the electric field intensity at C is $1.89 \times 10^7 \text{NC}^{-1}$ acting at 29.7° to horizontal.

Example 10



Three charges of $-3 \times 10^{-9} \text{C}$, $+4 \times 10^{-9} \text{C}$ and $+3 \times 10^{-8} \text{C}$ are placed at vertices A, B, C respectively of a rectangle ABCD of side 3 cm x 4 cm as shown. Calculate the resultant electric field intensity at D

Solution



E at D due to charge at A

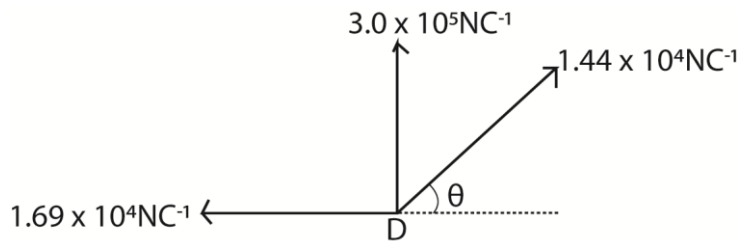
$$E_A = \frac{9 \times 10^9 \times 3 \times 10^{-9}}{(4 \times 10^{-2})^2} = 1.69 \times 10^4 \text{NC}^{-1}$$

E at D due to charge at B

$$E_B = \frac{9 \times 10^9 \times 4 \times 10^{-9}}{(5 \times 10^{-2})^2} = 1.44 \times 10^4 \text{NC}^{-1}$$

E at D due to charge at C

$$E_C = \frac{9 \times 10^9 \times 3 \times 10^{-8}}{(3 \times 10^{-2})^2} = 3.0 \times 10^5 \text{NC}^{-1}$$



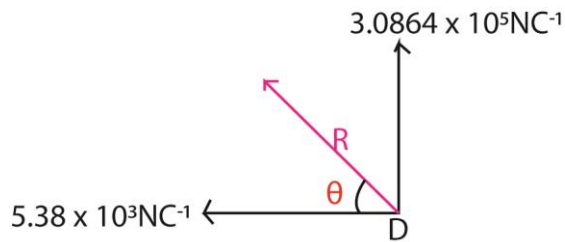
$$\sin \theta = \frac{3}{5} = 0.6; \quad \cos \theta = \frac{4}{5} = 0.8$$

Resolving vertically;

$$E_y = 3.0 \times 10^5 + 1.44 \times 10^4 \sin \theta$$
$$= 3.0864 \times 10^5 \text{ NC}^{-1}$$

Resolving horizontally

$$E_x = -1.69 \times 10^4 + 1.44 \times 10^4 \cos \theta$$
$$= -1.69 \times 10^4 + 1.44 \times 10^4 \times 0.8$$
$$= -5380 \text{ NC}^{-1}$$



$$R^2 = (3.0864 \times 10^5)^2 + (5380)^2$$

$$R = 3.09 \times 10^5 \text{ NC}^{-1}$$

$$\tan \theta = \frac{3.0864 \times 10^5}{5380}$$

$$\theta = 89^\circ$$

Hence electric field intensity at $D = 3.09 \times 10^5 \text{ NC}^{-1}$ at 89° to horizontal

Field strength and charge density