## Angles

In geometry, an angle can be defined as the figure formed by two straight lines meeting at a common end point.

An angle is represented by the symbol $\angle$. Here, the angle below is $\angle A O B$.

## Parts of an Angle:

Arms: The two rays joining to form an angle are called arms of an angle. Here, OA and OB are the arms of the $\angle A O B$.

Vertex: The common end point at which the two rays meet to form an angle is called the vertex. Here, the point $O$ is the vertex of $\angle A O B$.


Types of angle
Angles can be classified on the basis of their measurements as
An acute Angle is an angle that measures less than 90 degrees
A right Angle is an angle which is equal to $90^{\circ}$,
An obtuse Angle is an angle has a measurement greater than 90 degrees but less than 180 degrees.

A straight Angles is an angle is 180 degrees
A reflex Angles is an angle that is more than 180deg but less than 360deg
A complete Angle is a straight line makes an angle of 360 。


Interior and Exterior Angles:


## Interior angle

- An interior angle of a polygon is an angle inside the polygon at one of its vertices.
- The sum of the measures of the interior angles of a polygon with $n$ sides is ( $n-$ 2)180.
- The measure of each interior angle of an equiangular $n$-gon is $\frac{(n-2) 180}{n}$ or $180-\frac{360}{n}$ (the supplement of an exterior angle).


## Exterior angle

- An exterior angle of a polygon is an angle outside the polygon formed by one of its sides and the extension of an adjacent side.
- If you count one exterior angle at each vertex, the sum of the measures of the exterior angles of a polygon is always $360^{\circ}$.


## The measure of each exterior angle of an equiangular $n$-gon is $\frac{360}{n}$.

## Terms related to sum of angles

Complementary angles add up to $90^{\circ}$

$a+b=90^{\circ}$
thus $a$ and $b$ are complementary angles
Supplementary angles add up to $\mathbf{1 8 0}^{\mathbf{0}}$


$$
a+b+c+d=180^{\circ}
$$

## thus, a, b, c, and $d$ are supplementary angles

## Polygons

Polygons are usually defined by the number of sides that they have.
(a) A triangle

Is a three-sided polygon. Triangles can be defined by the length of the sides.
(i) Equilateral triangle has all sides equal and all its internal angles are $60^{\circ}$.
(ii) Isosceles triangle has two equal sides, with the third one a different length. Two of the internal angles are equal
(iii) Scalene triangle has all the three sides and all the three internal angles different
(iv) Right angled triangle has one of the angle $=90^{\circ}$
(v) All internal angles of triangles add up to $180^{\circ}$.


## Quadrilaterals

This are four-sided polygons

The internal angles of all quadrilaterals add up to $360^{\circ}$.
They include the square, rectangle, rhombus, parallelograms, trapezium and kite
(i) Square: all its sides are equal and each of its internal angles is equal to 900
(ii) Rectangle: has four internal angles each equal to 900 and equal opposite sides
(iii) Parallelogram has equal opposite sides and angles
(iv) Rhombus has all sides equal and equal opposite angles
(v) Trapezium: has two parallel sides and unequal angle
(vi) Kite has two pairs of equal adjacent sides, the shape has an axis of symmetry

## Quadrilaterals



## Parallel lines

These are lines that are always same distance apart and will never meet.
Transversal line is a line that cuts through two or more parallel lines
The following about parallel lines are equal


Equal angles
Alternative angles are: $\mathrm{d}-\mathrm{e}, \mathrm{c}-\mathrm{f}, \mathrm{b}-\mathrm{g}, \mathrm{a}-\mathrm{h}$ corresponding angles: $\mathrm{a}-\mathrm{e}, \mathrm{b}-\mathrm{f}, \mathrm{c}-\mathrm{g}, \mathrm{d}-\mathrm{h}$
Verticle angles: $a-d, b-c, e-h, f-g$

## Revision questions

1. In the diagram below, what is angle a?

2. In the diagram below, find the size of angle $x$

3. In the diagram below, which of the angles, $Q, R$ is the same as the angle marked a?

4. In the triangle $D B F$, angle $D E F=60^{\circ}$ and angle $D F E=42^{\circ}$. Find the size of angle DSE.

5. In the diagram below, which of the angles, $Q, R$ is the same as the angle marked $a$ ?

6. In the diagram below, LM is parallel to PQ . Find the Value of x .

7. In the figure below, find the value of angle $x$

8. Find the size of the angle marked $x$ in the figure below. $B C$ is parallel to $A D$.

9. The figure below is an isosceles triangle, find the value of $x$.

10. In the figure below, find the size of angle marked $x$.

11. Find the size of the angle marked $S$ in the figure below:

12. In the figure below, $B C D$ is a triangle and $A B C$ is a straight line; Find the value of $t$.

13. Find the value of the angle marked $(2 x+10)^{\circ}$ in the figure below:

14. Find the value of angle $P$ in the figure below:

15. Find the value of $x$ in the figure below.

16. In the diagram below $A E$ is parallel to $C D$. Find the size of angle $r$.

17. In the diagram below, $A B C$ is an isosceles triangle. Find the value of $P$ at $A$

18. Find the value of $x$ in the figure below.

19. Find the value of $x$ in the figure below

20. Study the triangle below and use it to answer the questions that follow. A

i) Find the value of $t$.
21. Find the value of the angle marked $p$ in the figure below.

22. Find the complement of an angle of $70^{\circ}$.
23. Find the size of angle $v$ in the figure below.

24. Two angles are supplementary. If one of them is $28^{\circ}$, find the other angle.

25 . Find the value of $x$ in the figure below.

26. In the diagram below, XTS is parallel to PYQR. Use it to find the size of angle $Z$.

27. Find the complement of the angle of $25^{\circ}$
28. In the triangle $P Q R$, angle $P Q R=78^{\circ}$, angle $P R Q=42^{\circ}$ and angle $P Q S=32^{\circ}$. Find the size of angle PSQ.

29. Find the size of one of the exterior angles of a regular octagon.
30. In the figure below, $A B$ is parallel to $C D$, find the value of $x$

31. The figure below is an isosceles triangle. Find the size of angle $x$

32. Find the valve of $Y$ in the figure below.

33. Find the value of $x$ in the figure below.

34. In the diagram below, PTUV is a straight line, angle $T S U=40^{\circ}$, angle $S U V=150^{\circ}$ and angle $P Q T=30^{\circ}$.use the given information to find the value o the angle marked k and n .
(04 marks)

35. Find the value $w$ in the figure below

36. In the diagram below, $C A B$ is a triangle and $D C A$ a triangle line. Study it and answer the question below(3marks)
(a) What is the valve of $Y$ ?

(b) What the size of angle ACB?
37. In the figure below, find the value of $n$ in degrees.

38. In the triangle below, find the size of angle g in degrees.

39. In the diagram below, OP is parallel to $\mathrm{QR}, \mathrm{HKL}$ is triangle, angle $\mathrm{HLR}=110^{\circ}$ and angle SHP $=50^{\circ}$

Study it and answer the questions that follow.


Find the size of
(a) Angle y:
(b) angle M
40. In the diagram below, find the valve of x .

41. In the figure below, find the bearing of town $B$ from town $A$.

42. 36 In the diagram below, line $A B$ is parallel to $C D$ and $B C D$ is an isosceles triangle. Study it carefully and use it to answer the questions that follow.

(a) Find the value of $X$
(b) Work out the size of angle $A B C$
43. In the diagram below, find the valves of $K$

(a) The interior angle of a regular polygon is 36 more than its exterior angle. What is the size of each exterior angle?
(b) In the figure below $D E$ is parallel to $F G$, angle $O D E=127^{\circ}$ and angle $O F G=136^{\circ}$. Calculate the size of angle $x$.

44. Find the value of $X$ in the diagram below.

45. In the figure below, $B C D$ is a straight line. Line $B X$ bisects angle $A B C$. Line $A B$ is parallel to line $X C$. Angle $B C E=50^{\circ}$ and angle $B A C=70^{\circ}$


Find the size of the angles:
(i) CEX
(04 marks)
(ii) $D C X$
(01 marks)
46. Find the size of angle $y$ the figure below.

47. In the figure below line $A B$ is parallel to $C D$, Angle CTV $=44$ and angle TQR=56. Study use it to answer the questions that follow:


Find the size of
(a) Angle $k$
(02mark)
(b) Angle g
(02mark)
48. In the triangle below, find the value of $d$ in degrees

49. Study the figure below and use it to answer the questions that follow.

(a) Find the value of $g$ (03marks)
(b) Calculate the size of angle RST
50. Find the value of $p$ in degrees in the diagram below

51. (a) The interior angle of a regular polygon is 108 more than the exterior angle. How many sides has the polygon? (03marks)
(b) Find size of angle $z$ in the figure below

52. In the diagram below, line $D H$ is parallel to $F E$. Angle $A C B=75^{\circ}$ and angle $C B E=135^{\circ}$. Angle FAD is twice angle DAC. Study the diagram and use it to answer the questions that follow.

(b) Find the size of angle A

## Suggested solution

1. In the diagram below, what is angle a?


$$
\begin{aligned}
& 55^{\circ}+55^{\circ}+a=180^{\circ} \text { (angle sum of triangle) } \\
& 110^{\circ}+a=180^{\circ} \\
& 110^{\circ}-110^{\circ}+a=180^{\circ}-110^{\circ} \\
& a=70^{\circ}
\end{aligned}
$$

2. In the diagram below, find the size of angle $x$


## Solution

$$
\begin{gathered}
60^{0}+x=110^{0} \\
60^{\circ}-60^{\circ}+x=110^{0}-60^{0} \\
x=50^{0}
\end{gathered}
$$

3. In the diagram below, which of the angles, $Q, R$ is the same as the angle marked a?


Solution
$R$ (vertical angles are equal)
4. In the triangle DBF, angle $\operatorname{DEF}=60^{\circ}$ and angle $\mathrm{DFE}=42^{\circ}$. Find the size of angle DSE.


Finding angle EDF first,
$\angle E D F+42^{\circ}+60^{\circ}=180^{\circ}$
$\angle \mathrm{EDF}+102^{\circ}=180^{\circ}$
<EDF $+102^{\circ}-102^{\circ}=180^{\circ}-102^{0}$
$\angle E D F=78^{\circ}$
Now $\angle \mathrm{DSE}+78^{\circ}+30^{\circ}=180^{\circ}$
$<$ DSE $+108^{\circ}=180^{\circ}$
$\angle D S E+108^{\circ}-108^{\circ}=180^{\circ}-108^{\circ}$
$\angle D S E=72^{\circ}$
5. In the diagram below, which of the angles, $Q, R$ is
the same as the angle marked a ?


Solution
Q (vertical angles are equal)
6. In the diagram below, LM is parallel to PQ . Find the Value of x .


$$
\begin{aligned}
& <P Q L=<Q L M=50^{\circ} \\
& \quad \Rightarrow 60^{\circ}+50^{\circ}+\mathrm{x}=180^{\circ} \text { (angle sum of triangle) } \\
& \quad \Rightarrow \mathrm{x}=180^{\circ}-\left(110^{\circ}\right) \\
& \quad \Rightarrow \mathrm{x}=70^{\circ}
\end{aligned}
$$

7. In the figure below, find the value of angle $x$


Angle $\mathrm{BAC}=$ angle ACB

$$
\begin{aligned}
30^{\circ}+x+x & =180^{\circ} \\
30^{\circ}+2 x & =180^{\circ} \\
2 x & =180^{\circ}-30^{\circ} \\
x & =75^{\circ}
\end{aligned}
$$

8. Find the size of the angle marked $x$ in the figure below. $B C$ is parallel to $A D$.


$$
\begin{aligned}
84+x & =180 \\
x & =180-84 \\
& =96^{\circ}
\end{aligned}
$$

9. The figure below is an isosceles triangle, find the value of $x$.


$$
\begin{aligned}
& 4 x=x+30 \\
& 4 x-x=30 \\
& 3 x=30 \\
& x=10^{0}
\end{aligned}
$$

10. In the figure below, find the size of angle marked $x$.


$$
\begin{array}{r}
<B A C=<A C B=180-130=50^{\circ} \\
<B A C+<A C B+x=180^{\circ} \text { (angle sum } \\
\text { of triangle) }
\end{array}
$$

$$
\begin{array}{r}
50^{\circ}+50^{\circ}+x=180^{\circ} \\
x=80^{\circ}
\end{array}
$$

11. Find the size of the angle marked $S$ in the figure below:

$59+S+63=180^{\circ}$ (angle sum of straight line

$$
\begin{aligned}
122+S & =180^{\circ} \\
S & =58^{\circ}
\end{aligned}
$$

12. In the figure below, $B C D$ is a triangle and $A B C$ is a straight line; Find the value of $t$.

$7 t+5 t=180^{\circ}$ (angle sum of a straight line)

$$
\begin{aligned}
12 t & =180^{\circ} \\
t & =15^{\circ}
\end{aligned}
$$

13. Find the value of the angle marked $(2 x+10)^{\circ}$ in the figure below:


The sum of two opposite anterior angles= exterior angles
$(2 x+10)+x=x+70$
Remove brackets
$2 \mathrm{x}+10+\mathrm{x}=\mathrm{x}+70$
Collect like terms
$2 x=60^{\circ}$
$\mathrm{X}=30$
The required angle $=2 \mathrm{x}+10=2 \times 30+10=70^{\circ}$
14. Find the value of angle $P$ in the figure below:


Two opposite interior angles = exterior angle

$$
\begin{aligned}
40+P & =70 \\
P & =30^{\circ}
\end{aligned}
$$

15. Find the value of $x$ in the figure below.

16. In the diagram below $A E$ is parallel to $C D$. Find the size of angle $r$.

$40^{\circ}+65^{\circ}+\angle E B D=180^{\circ}$ (angle sum of straight line)

Angle EBD $=180^{\circ}-(40+65)^{\circ}$
$=75^{\circ}$
$r=$ angle $E B D=75^{\circ}$ (alternative angles)
17. In the diagram below, $A B C$ is an isosceles triangle. Find the value of $P$ at $A$


$$
\begin{aligned}
& \angle \mathrm{ACB}+130=180 \text { (angle sum on straight line) } \\
& \text { Angle } \mathrm{ACB}=180-130=50^{\circ} \\
& \angle \mathrm{ABC}=\angle \mathrm{ACB}=50^{\circ} \\
& \mathrm{P}+\angle \mathrm{ABC}+\angle \mathrm{ACB}=180^{\circ} \\
& \mathrm{P}+50+50=180^{\circ} \\
& P=80^{\circ}
\end{aligned}
$$

18. Find the value of $x$ in the figure below.


$$
\begin{aligned}
x+2 x & =90^{\circ} \\
3 x & =90^{\circ} \\
x & =30^{\circ}
\end{aligned}
$$

19. Find the value of $x$ in the figure below


$$
(2 x-3)=(x+5)
$$

Remove brackets

$$
2 x-3=x+5
$$

$$
x=8
$$

20. Study the triangle below and use it to answer the questions that follow. A

iii) Find the value of t .

$$
(3 t+18)+(5 t+18)+80^{\circ}=180^{\circ} \text { (angle sum of triangle) }
$$

Remove brackets

$$
\begin{aligned}
3 t+18+5 t+18+80 & =180 \\
8 t+116 & =180 \\
8 t & =64 \\
t & =8^{0}
\end{aligned}
$$

iv) Find the size of angle $A B C$.

$$
\text { Angle } A B C=5 \times 8+18=58^{0}
$$

21. Find the value of the angle marked $p$ in the figure below.


$$
\begin{aligned}
70+P & =180^{\circ} \text { (angle sum of a triangle) } \\
P & =110^{\circ}
\end{aligned}
$$

22 . Find the complement of an angle of $70^{\circ}$.

$$
\begin{array}{r}
70^{\circ}+\text { complement }=90^{\circ} \\
\text { Complement }=20^{\circ}
\end{array}
$$

23. Find the size of angle $y$ in the figure below.

24. Two angles are supplementary. If one of them is $28^{\circ}$, find the other angle.

Supplementary angles add up to $180^{\circ}$
$\therefore$ the supplement of $280=(180-28)^{0}=152^{\circ}$

25 . Find the value of $x$ in the figure below.

26. In the diagram below, XTS is parallel to PYQR. Use it to find the size of angle Z.


$$
\begin{aligned}
& \angle T Y Q=\angle T Q Y=70^{\circ} \text { (alternative angle) } \\
& \angle T Y Q+\angle T Q Y+Z=180^{\circ} \text { (angle sum of triangle) } \\
& 70^{\circ}+70^{\circ}+Z=180^{\circ} \\
& 140^{\circ}+Z=180^{\circ} \\
& \quad Z=40^{\circ}
\end{aligned}
$$

27. Find the complement of the angle of $25^{\circ}$

Complementary angles add up to $90^{\circ}$

Let the angle be $y$

$$
\begin{aligned}
y+250 & =90^{\circ} \\
y & =65^{\circ}
\end{aligned}
$$

28. In the triangle $P Q R$, angle $P Q R=78^{\circ}$, angle $P R Q=42^{\circ}$ and angle $P Q S=32^{\circ}$. Find the size of angle $P S Q$.


$$
\text { Angle QPR + angle PQR + angle QRP = } 180^{\circ} \text { (angle sum of a triangle) }
$$

$$
\text { Angle QPR }+78^{\circ}+42^{\circ}=180^{\circ}
$$

$$
\text { Angle } \mathrm{QPR}=60^{\circ}
$$

Angle $\mathrm{PSQ}+$ angle $\mathrm{QPS}+$ angle $\mathrm{PQS}=180^{\circ}$ (angle sum of a triangle)

$$
\text { Angle PSQ }+60^{\circ}+32^{\circ}=180^{\circ}
$$

$$
\text { Angle PSQ = } 88^{\circ}
$$

29. Find the size of one of the exterior angles of a regular octagon.

$$
\text { Exterior angle }=\frac{360}{\text { number of sides }}=\frac{360}{8}=45^{\circ}
$$

30. In the figure below, $A B$ is parallel to $C D$, find the value of $x$


$$
\begin{aligned}
& 3 x=60^{\circ} \text { (alternative angle) } \\
& \frac{3 x}{3}=\frac{60^{0}}{2} \\
& x=20^{\circ}
\end{aligned}
$$

31. The figure below is an isosceles triangle. Find the size of angle $x$


Angle $C A B=$ angle $A B C=x$
It implies that: $x+x+40=180^{\circ}$ (angle sum of a triangle)

$$
\begin{array}{r}
2 x+40=180 \\
2 x=140 \\
x=70^{\circ}
\end{array}
$$

32. Find the valve of $Y$ in the figure below.


$$
\text { Interior angle }+ \text { exterior angle }=180^{\circ}
$$

$$
\begin{aligned}
Y+125 & =180^{\circ} \\
Y & =55^{\circ}
\end{aligned}
$$

33. Find the value of $x$ in the figure below.


Angle sum on a straight line add up to $180^{\circ}$.
$90+28+2 x=180$
$118+2 x=180$

$$
\begin{aligned}
2 x & =180-118 \\
& =62^{\circ}
\end{aligned}
$$

$$
x=31^{0}
$$

34. In the diagram below, PTUV is a straight line, angle $T S U=40^{\circ}$, angle $S U V=150^{\circ}$ and angle $P Q T=30^{\circ}$.use the given information to find the value o the angle maerked k and n .

35. Find the value $w$ in the figure below


$$
\begin{aligned}
W+35 & =180 \\
W & =180-35 \\
& =145^{\circ}
\end{aligned}
$$

36. In the diagram below, $C A B$ is a triangle and $D C A$ a triangle line. Study it and answer the question below(3marks)
(a) What is the valve of $Y$


$$
\begin{aligned}
4 y+20 & =y+5+2 y+25 \\
y & =10^{0}
\end{aligned}
$$

(c) What the size of angle ACB?

$$
\begin{aligned}
\text { angle } A C B & =180^{\circ}-(4 y+20) \\
& =180^{\circ}-(4 \times 10+20) \\
& =120^{\circ}
\end{aligned}
$$

37. In the figure below, find the value of n in degrees.

$108+n=180$

$$
n=72^{\circ}
$$

38. In the triangle below, find the size of angle $g$ in degrees.

39. In the diagram below, OP is parallel to $\mathrm{QR}, \mathrm{HKL}$ is triangle, angle $\mathrm{HLR}=110^{\circ}$ and angle $\mathrm{SHP}=50^{\circ}$

Study it and answer the questions that follow.


Find the size of
(c) Angle y:

Angle SKI $=$ angle $\mathrm{SHP}=50^{\circ}$ (corresponding angle)
Angle y + angle SKI $=180^{\circ}$ (angle sum on a straight line)

$$
\begin{aligned}
y+50^{\circ} & =180^{0} \\
y & =130^{\circ}
\end{aligned}
$$

(d) angle M

Angle HIK $+110^{\circ}=180^{\circ}$ (angle sum on a straight line)

$$
\text { Angle } \mathrm{HIK}=70^{\circ}
$$

Angle HIK + angle HKI $+\mathrm{m}=180^{\circ}$ (angle sum of triangle)

$$
\begin{aligned}
70^{0}+50^{0}+\mathrm{m} & =180^{0} \\
\mathrm{~m} & =60^{0}
\end{aligned}
$$

40. In the diagram below, find the valve of x .


$$
\begin{array}{r}
55+x=90^{\circ} \\
x=35^{\circ}
\end{array}
$$

41. In the figure below, find the bearing of town $B$ from town $A$.

42. 36 In the diagram below, line $A B$ is parallel to $C D$ and $B C D$ is an isosceles triangle. Study it carefully and use it to answer the questions that follow.

(c) Find the value of $X$
(3marks)
Angle $B C D=$ Angle $C D B=3 x^{0}$ (corresponding angles)

$$
\begin{aligned}
7 x^{0}+3 x^{0} & =180 \text { (angle sum of a straight line) } \\
X & =18^{0}
\end{aligned}
$$

(d) Work out the size of angle $A B C$

$$
\text { Angle } A B C=\text { angle } B C D \text { (alternate angles) }=3 x^{0}=18 \times 3=54^{\circ}
$$

43. In the diagram below, find the valves of $K$

$50^{\circ}+k+50^{\circ}=180^{\circ}$ (angle sum of a straight line)

$$
k=80^{\circ}
$$

. (a) The interior angle of a regular polygon is 36 more than its exterior angle. What is the size of each exterior angle?

Let the exterior angle be $x$
The anterior angle $=x+36$

$$
\text { Then, } \begin{array}{r}
x+x+36=180 \\
x=72
\end{array}
$$

(b) In the figure below DE is parallel to FG, angle ODE $=127^{\circ}$ and angle OFG $=136^{\circ}$. Calculate the size of angle $x$.

44. Find the value of $X$ in the diagram below.


$$
\begin{aligned}
3 x+90^{\circ}+2 x & =180^{\circ} \text { (angle sum of straight line) } \\
x & =18^{\circ}
\end{aligned}
$$

45. In the figure below, $B C D$ is a straight line. Line $B X$ bisects angle $A B C$. Line $A B$ is parallel to line $X C$. Angle $B C E=50^{\circ}$ and angle $B A C=70^{\circ}$


Find the size of the angles:
(iii) CEX

Considering triangle $A B C$
$a+a+50^{\circ}+70^{\circ}=180^{\circ}$ (angle sum of a triangle)
$2 \mathrm{a}=60^{\circ}$
$A=30^{\circ}$

Using triangle $B A E$
$a+$ Angle BEA $+70^{\circ}=180^{\circ}$
$30^{\circ}+$ angle $B E A+70^{\circ}=180^{\circ}$
Angle BEA $=80^{\circ}$
But, angle BEA = angle CEK
$\therefore$ Angle CEK $=80^{\circ}$
(iv) DCX

$$
\begin{aligned}
& \text { Angel } X C A=\text { angle } B A C=70^{\circ} \text { (alternative angles) } \\
& \text { Angle } B C A+\text { angle } A C X+\text { angle } X C D=180^{\circ} \text { (angle sum on a straight line) }
\end{aligned}
$$

$$
50^{\circ}+70^{\circ}+\text { angle } X C D=180^{\circ}
$$

46. Find the size of angle $y$ the figure below.

47. In the figure below line $A B$ is parallel to $C D$, Angle $C T V=44$ and angle $T Q R=56$. Study use it to answer the questions that follow:


Find the size of
(c) Angle $k$

Angle RTD $=44^{\circ}$ (corresponding angles)
Angle RTD $+\mathrm{k}+56=180$

$$
k=180-(44+56)=80^{\circ}
$$

(d) Angle g

$$
\begin{aligned}
\mathrm{g}+\text { angle } \mathrm{RTD} & =180^{\circ} \\
\mathrm{g} & =180-44=136^{\circ}
\end{aligned}
$$

48. In the triangle below, find the value of $d$ in degrees

$5 \mathrm{~d}=180$ (angle sum of a triangle)
$d=36^{\circ}$
49. Study the figure below and use it to answer the questions that follow.

(c) Find the value of $g$ (03marks)

$$
\begin{aligned}
(3 \mathrm{~g}+6)+(\mathrm{g}+30)+(2 \mathrm{~g}-24) & =180^{\circ} \text { (angle sum of a triangle) } \\
3 \mathrm{~g}+6+\mathrm{g}+30+2 \mathrm{~g}-24 & =180^{\circ} \\
6 \mathrm{~g}+12 & =180^{\circ} \\
6 \mathrm{~g} & =192^{\circ} \\
\mathrm{g} & =32^{\circ}
\end{aligned}
$$

(d) Calculate the size of angle RST

$$
\begin{aligned}
\text { Angle RST } & =(\mathrm{g}+30)^{0} \\
& =32+30 \\
& =62^{\circ}
\end{aligned}
$$

50. Find the value of $p$ in degrees in the diagram below

$180-5 p+180-3 p+180-4 p=180$ (angle sum of triangle)

$$
\begin{aligned}
540-12 p & =180 \\
12 p & =360 \text { (sum of exterior angle) } \\
p & =30^{\circ}
\end{aligned}
$$

51. (a) The interior angle of a regular polygon is 108 more than the exterior angle. How many sides has the polygon? (03marks)

Let exterior angle be $x$

$$
\begin{aligned}
x+x+108^{\circ} & =180^{\circ} \text { (angle sum of straight line) } \\
x & =36^{\circ}
\end{aligned}
$$

Number of sides $=360 / 36=10$ sides
(b) Find size of angle $z$ in the figure below


$$
\begin{gathered}
55^{\circ}+60^{\circ}+z=180^{\circ} \text { (angle sum of a triangle) } \\
z=65^{\circ}
\end{gathered}
$$

52. In the diagram below, line DH is parallel to FE . Angle $\mathrm{ACB}=75^{\circ}$ and angle $\mathrm{CBE}=135^{\circ}$. Angle FAD is twice angle DAC. Study the diagram and use it to answer the questions that follow.

(c) Calculate the size of angle DAC
(03marks)

Angle CBA + angle CBE $=180^{\circ}$ ( angle sum of a straight line)

$$
\begin{aligned}
\text { Angle CBA } & =(180-135)^{0} \\
& =45^{\circ}
\end{aligned}
$$

Then angle $A C B+$ angle $C A B+$ angle $A B C=180^{\circ}$ (angle sum of a triangle)
(d) Find the size of angle DAC

Angle $\mathrm{DAC}=$ angle $\mathrm{FAD}=2 \mathrm{X}=2 \times 40=80^{\circ}$ (corresponding angles)

Thank you

